

Solutions

Problem 1:

(A) Phase and group velocity: phase velocity: ω/k , group velocity: $d\omega/dk$.
Information (energy) moves with a speed equal to the group velocity.

Problem 2:

(E) Phase and group velocity: phase velocity: ω/k , group velocity: $d\omega/dk$.
 $d\omega/dk = c^2k / (c^2k^2 + m^2)^{1/2}$

Problem 3:

(B) Doppler shift:

For the end moving towards the observer:

$$f'_1 = f[(1+v/c)/(1-v/c)]^{1/2} \approx f[1+v/c]$$

For the end moving away from the observer:

$$f'_2 = f[(1-v/c)/(1+v/c)]^{1/2} \approx f[1-v/c]$$

Therefore $\Delta f = f'_1 - f'_2 = 2f v/c$.

$$v = (\Delta f/f)c/2 = (\Delta\lambda/\lambda)c/2 = (1.8 \cdot 10^{-12}/1.22 \cdot 10^{-7}) \cdot 1.5 \cdot 10^8 = 2213 \text{ m/s} = 2.2 \text{ km/s}$$

Problem 4:

(B) Polarization: For plane polarization the x- and y-components of \mathbf{E} are in phase or 180° out of phase.

Problem 5:

(A) Vector addition.

After a path difference of $2\pi/k = \lambda$ the phases of the x and y components still differ by π .

Problem 6:

(D) This answer is not a solution to the wave equation $\partial^2 f/\partial t^2 = v^2 \partial^2 f/\partial x^2$, i.e. it is not a linear superposition of solutions of the form $f(x,t) = f(x \pm vt)$.

Problem 7:

(B) Mirrors and thin lenses: $1/x_o + 1/x_i = 1/f$, $M = -x_i/x_o$.