

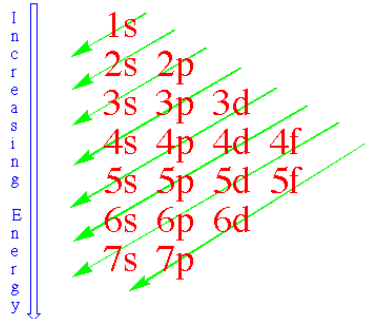
Problem 1: (C)

Uncertainty principle

$$\Delta E \Delta t \sim \hbar, \Delta E \sim \hbar / \Delta t \sim (10^{-34} \text{ Js} * 1 \text{ eV} / 1.6 * 10^{-19} \text{ J}) / (5 * 10^{-9}) = 2 * 10^{-7} \text{ eV}$$

Problem 2: (A)

The electron subshells of atoms in their ground state are filled one electron at a time by putting each electron into the state with the lowest available energy. The energy ordering of the subshells can be remembered from the diagram below.



Problem 3: (D)

Energy stored in a capacitor, $U = \frac{1}{2} Q^2/C$

With the plates isolated, charge cannot be added or removed. An external force must do work to remove the dielectric.

Problem 4: (A)

The Lorentz force

$$\mathbf{F} = q\mathbf{v} \times \mathbf{B} = 0.$$

Problem 5: (B)

Thin lenses

$$1/x_i = 1/f - 1/x_o = 1/4 - 1/3 = -1/12, x_i = -12, M = -x_i/x_o = 12/3 = 4.$$

Problem 6: (C)

The 1D Harmonic oscillator in QM

Problem 7: (B)

Energy conservation

$$\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{\sqrt{x^2 + y^2}} = \frac{1}{2} mv^2$$

$$\text{In SI units: } 9 * 10^9 * 10^{-11} / (5 * 10^{-2}) = \frac{1}{2} * 10^{-3} * v^2.$$

Problem 8: (D)

Terminal speed: $F_{\text{total}} = 0$

$$mg = \beta v.$$

Problem 9: (B)

Power, $P = dE/dt$

$dE/dt = mv \, dv/dt$, dv/dt is proportional to $1/v$ neglecting friction and drag.

Problem 10: (D)

Angular momentum

$L = I\omega$, $I = \frac{1}{2}Mr^2 + MR^2$.

Problem 11: (A)

Conservation of angular momentum

Problem 12: (A)

The hydrogen atom

Problem 13: (C)

Spin $\frac{1}{2}$ particles

Problem 14: (A)

Bernoulli's theorem

$$\frac{1}{2} \rho v_1^2 + P_1 + \rho g h_1 = \frac{1}{2} \rho v_2^2 + P_2 + \rho g h_2$$

Problem 15: (D)

Rayleigh scattering

Problem 16: (E)

Multiple "slit" interference

$d \sin \theta = n\lambda = nc/f = n \cdot 3 \cdot 10^8 / 10^6 \text{ m} = n \cdot 300 \text{ m}$, $d/2 = n \cdot 300 \text{ m}$.

Problem 17: (B)

Harmonic motion, a mass on a spring

For a single mass m on a massless spring with spring constant k we have $\omega = (k/m)^{1/2}$.

Problem 18: (B)

Lagrangian mechanics, cyclic coordinates

If q_n is a cyclic coordinate then $dp_n/dt = 0$. (Lagrangian formalism: $p_n = \frac{\partial L}{\partial \dot{q}_n}$).

Problem 19: (D)

Relativistic energy and momentum

$pc = \gamma mvc = 5 \text{ MeV}$; $E = \gamma mc^2 = 10 \text{ MeV}$; $pc/E = v/c = \frac{1}{2}$

Problem 20: (D)

The electric potential, the principle of superposition

$$V = k \int_0^1 \lambda dx / (2l-x) = (kQ/l) \int_0^1 dx / (2l-x) = (kQ/l) \int_1^{2l} dx' / x' = (kQ/l) \ln 2$$

Problem 21: (C)

Entropy

A reversible process does not change the entropy of the system.

Problem 22: (E)

Linear polarizers

$$I_t = I_0 \cos^2 \theta, \text{ (Law of Malus) for a single polarizer}$$

Problem 23: (D)

Commutator algebra, commutation rules for angular momentum

$$[J_x J_y, J_x] = J_x [J_y, J_x] + [J_x, J_x] J_y = -i\hbar J_x J_z$$

Problem 24: (B)

Momentum conservation

$$4m\sqrt{2gh} - m\sqrt{2g \cdot 4h} = 5mv, \quad v = \frac{2}{5}\sqrt{2gh}$$

Problem 25: (D)

Rotational kinetic energy, $T_{\text{rot}} = \frac{1}{2} I\omega^2$.

$$\Delta T_{\text{rot}} = 2(80^2 - 40^2)\text{J} = 9600 \text{ J}$$