

Problem 1: (D)

Relativistic energy: $E^2 = p^2c^2 + m^2c^4$, $p^2c^2 = (10^4 - 1)m^2c^4$, $pc \sim 100 mc^2$.

Problem 2: (B)

Energy and momentum conservation:

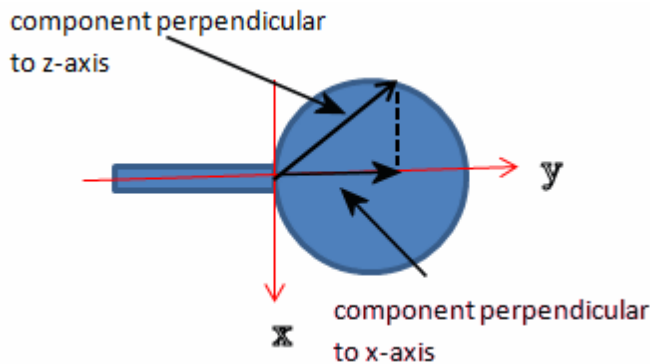
$$Mc^2 = (m^2c^4 + p^2c^2)^{1/2} + pc, \quad M^2c^4 - 2Mpc^3 = m^2c^4, \quad p = (M^2 - m^2)c/(2m)$$

Problem 3: (B)

Length contraction: $L' = L/\gamma$, $\gamma = (1 - 0.64)^{-1/2} = 1/0.6$. $t = (0.6 \text{ m})/(0.8 \cdot 3 \cdot 10^8 \text{ m/s}) = 2.5 \text{ ns}$

Problem 4: (D)

Moment of inertia about an axis: $I = \sum m_i r_i^2$ I_y is the smallest



Problem 5: (D)

Hamilton's equations of motion: $q_i = \frac{\partial H}{\partial p_i}$, $\dot{p}_i = -\frac{\partial H}{\partial q_i}$

Problem 6: (D)

The Lagrangian $L = T - U$: $T = \frac{1}{2}M\dot{X}^2 + \frac{1}{2}m(\dot{X} + \dot{x})^2$, $U = \frac{1}{2}kx^2$.

Problem 7: (C)

Relativistic energy: $E^2 = p^2c^2 + m^2c^4 = 16 m^2c^4$, $p^2c^2 = 15 m^2c^4$, $pc = 15^{1/2} mc^2$.

Problem 8: (A)

Conservation of angular momentum: A central force conserves angular momentum. Kepler's second law is a statement of angular momentum conservation.

Problem 9: (B)

Length contraction and velocity addition: $L' = L/\gamma$, $1/\gamma = 0.6 = (1 - v^2/c^2)^{1/2}$, $v = 0.8 c$ is the speed of one spaceship with respect to the other.

$$0.8 c = (v' + v)/(1 + v'^2/c^2). \quad 0.8 + 0.8 v'^2/c^2 = 2 v'/c. \quad v'/c = 0.5$$

Problem 10: (B)

Transformation of the electromagnetic fields

Problem 11: (C)

Time dilation: $t = \gamma\tau$. $\gamma = (1 - v^2/c^2)^{-1/2}$, $\gamma = 5/3$, $t = (11/3) \cdot 10^{-6}$ s.

$$d = (4/5) \cdot 3 \cdot 10^8 \text{ m/s} \cdot (11/3) \cdot 10^{-6} \text{ s} = (44/5) \cdot 10^2 \text{ m}$$

Problem 12: (E)

Cyclic coordinates: The coordinate ϕ is cyclic, p_ϕ is a constant of motion.

Problem 13: (D)

The Lagrangian $L = T - U$: $T = \frac{1}{2}m(dr/dt)^2 + \frac{1}{2}mr^2(d\theta/dt)^2$, $U = \frac{1}{2}k(r-s)^2$

Problem 14: (C)

The Lorentz transformation:

In the frame O let event 1 have space-time coordinates $x = 0$, $t = 0$, and event 2 have space-time coordinates $x = 10$ m, $t = 0$. In O' let event 1 have $t' = 0$ and event 2 have $t' = -13$ ns.

The Lorentz transformation for event 2 gives $ct' = \gamma ct - \gamma\beta x$, $c \cdot 1.3 \cdot 10^{-8}$ s = $\gamma\beta \cdot 10$ m, $\gamma\beta = 0.39$.
 $\beta = 0.39 / (1 + 0.39^2)^{1/2} = 0.36$.

Problem 15: (A)

Kinematics: All quantities are given in the reference frame of the observer.