

Modern Physics, solutions

Problem 1:

(C) Uncertainty principle: $\Delta E \Delta t \sim \hbar$
 Δt = lifetime of the excited state

Problem 2:

(A) Bohr atom: All other answers are incorrect.

Problem 3:

(B) Dimensions of atoms and nuclei: You should know typical atomic and nuclear dimensions.

Problem 4:

(B) The infinite well: Know the energy eigenfunctions and eigenvalues of the infinite well.

Problem 5:

(C) Hydrogen atom and hydrogenic atoms:
 $E_n = -Z^2 \mu e^4 / (2\hbar^2 n^2)$, μ = reduced mass, E_n scales as $Z^2 \mu$.

Problem 6:

(A) Hydrogen atom: $E_n = -E_1/n^2$, longest Lyman: $E_2 - E_1$, longest Balmer: $E_3 - E_2$, ratio: $(1/4 - 1)/(1/9 - 1/4) = 27/5$. $\Delta E = hc/\lambda$. Wavelength ratio: 5/27

Problem 7:

(B) $KE = hf - \Phi = hc/\lambda - 2.28\text{eV} = 1.24 \cdot 10^4 \text{eV} \cdot \text{\AA} / 5000 \text{\AA} - 2.28\text{eV} = 0.2\text{eV}$

Problem 8:

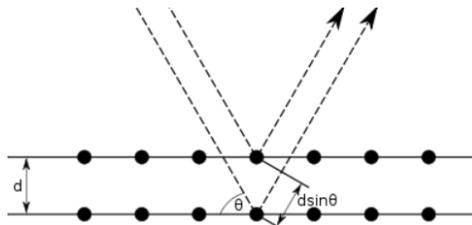
(E) Interpretation of the wave function:
 $P = \text{Integral } |\Psi(x)|^2 dx \text{ from } x = 2 \text{ to } x = 4$
 $P = N^2(4 + 9)$
 $1/N^2 = (1 + 1 + 4 + 9 + 1)$
 $P = 13/16$

Problem 9:

(C) The infinite well: The energy levels of the infinite well are proportional to n^2 . The $n = 2$ wave function is shown.

Problem 10:

(D) Bragg reflection:
 $2d \sin 30^\circ = \lambda = h/p = h/(mv)$



Problem 11:

(B) Operators:

In QM every observable is associated with its own operator.

For example: $p_x = (\hbar/i)\partial/\partial x$

Problem 12:

(B) The wave function: The wave function and its derivative must be continuous, the wave function must go to zero as x goes to infinity. The wave function oscillates in the classically allowed region and decays exponentially in the classically forbidden region.

Problem 13:

(B) The Pauli exclusion principle

Problem 14:

(C) The mean value of an observable: $\langle Q \rangle = \langle \Psi | Q | \Psi \rangle = \int_{-\infty}^{+\infty} \Psi^* Q \Psi dx$ in coordinate space in 1D.

Problem 15:

(D) The momentum operator: $(\hbar/i)\partial \exp(ikx)/\partial x = \hbar k \exp(ikx)$