

## Solutions

### Problem 1:

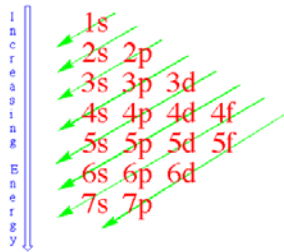
(C) **Uncertainty principle**

$$\Delta E \Delta t \sim \hbar, \Delta E \sim \hbar / \Delta t \sim (10^{-34} \text{ Js} * 1 \text{ eV} / 1.6 * 10^{-19} \text{ J}) / (5 * 10^{-9}) = 2 * 10^{-7} \text{ eV}$$

### Problem 2:

(A) **The periodic table**

The electron subshells of atoms in their ground state are filled one electron at a time by putting each electron into the state with the lowest available energy. The energy ordering of the subshells can be remembered from the diagram below.



### Problem 3:

(D) **Energy stored in a capacitor,  $U = \frac{1}{2} Q^2/C$**

With the plates isolated, charge cannot be added or removed. An external force must do work to remove the dielectric.

### Problem 4:

(A) **The Lorentz force**

$$\mathbf{F} = q\mathbf{v} \times \mathbf{B} = 0.$$

### Problem 5:

(B) **Thin lenses**

$$1/x_i = 1/f - 1/x_o = 1/4 - 1/3 = -1/12, x_i = -12, M = -x_i/x_o = 12/3 = 4.$$

### Problem 6:

(C) **The 1D Harmonic oscillator in QM**

### Problem 7:

(B) **Energy conservation**

$$[1/(4\pi\epsilon_0)]q_1q_2/(x^2 + y^2)^{1/2} = \frac{1}{2} mv^2.$$

$$\text{In SI units: } 9 * 10^9 * 10^{-11} / (5 * 10^{-2}) = \frac{1}{2} * 10^{-3} * v^2.$$

### Problem 8:

(D) **Terminal speed:  $F_{\text{total}} = 0$**

$$mg = \beta v.$$

**Problem 9:**(B) **Power,  $P = dE/dt$**  $dE/dt = mv dv/dt$ ,  $dv/dt$  is proportional to  $1/v$  neglecting friction and drag.**Problem 10:**(D) **Angular momentum** $L = I\omega$ ,  $I = \frac{1}{2}Mr^2 + MR^2$ .**Problem 11:**(A) **Conservation of angular momentum****Problem 12:**(C) **Spin  $\frac{1}{2}$  particles****Problem 13:**(A) **Bernoulli's equation** $P_1 + \rho gh_1 + \frac{1}{2}\rho v_1^2 = P_2 + \rho gh_2 + \frac{1}{2}\rho v_2^2$ **Problem 14:**(D) **Rayleigh scattering****Problem 15:**(E) **Multiple "slit" interference** $d \sin \theta = n\lambda = nc/f = n \cdot 3 \cdot 10^8 / 10^6 \text{ m} = n \cdot 300 \text{ m}$ ,  $d/2 = n \cdot 300 \text{ m}$ .**Problem 16:**(B) **Harmonic motion, a mass on a spring**For a single mass  $m$  on a massless spring with spring constant  $k$  we have  $\omega = (k/m)^{1/2}$ .**Problem 17:**(B) **Lagrangian mechanics, cyclic coordinates**If  $q_i$  is a cyclic coordinate then  $dp_i/dt = 0$ . (Lagrangian formalism:  $\partial L / \partial (dq_i/dt) = p_i$ )**Problem 18:**(D) **Relativistic energy and momentum** $pc = \gamma mvc = 5 \text{ MeV}$ ;  $E = \gamma mc^2 = 10 \text{ MeV}$ ;  $pc/E = v/c = \frac{1}{2}$ **Problem 19:**(C) **Entropy**

A reversible process does not change the entropy of the system.

**Problem 20:**(E) **Linear polarizers** $I_t = I_0 \cos^2 \theta$ , (Law of Malus) for a single polarizer