

Problem 1:

(B) **Kepler's third law:** $(T_1/T_2)^2 = (R_1/R_2)^3$. $(1440/80)^2 = (aR_E/R_E)^3$. $a = 6.87$.

Problem 2:

(A) **Rolling:** $\omega = v/R$. Energy conservation: $\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh$. $\omega^2 = gh/R^2$.

$$L = mR^2\omega = mR(gh)^{1/2}.$$

Problem 3:

(B) **Harmonic oscillator:** $T + U = \text{constant}$, $\omega^2 = k/m$.

$$\frac{1}{2}kA^2 = \frac{1}{2}mv^2 + (1/8)kA^2. \quad v = (3k/(4m))^{1/2} A = (3^{1/2}/2)\omega A = 3^{1/2}\pi fA$$

Problem 4:

(A) **The total angular momentum is conserved in a collision between two interacting objects.**

Total angular momentum about the point P before the collision:

$$L = I\omega - MvR = \frac{1}{2}MR^2 \cdot 2v/R - MvR = 0.$$

Problem 5:

(C) **Harmonic oscillator potential:** $U(x) = \frac{1}{2}kx^2 + \text{constant}$, $\omega^2 = k/m$.

Problem 6:

(E) **F = dp/dt**, $dp = p(t+dt) - p(t) = (m-|dm|)(v+dv) + |dm|(v-u) - mv = m dv - |dm|u$.

Problem 7:

(E) **Solving a differential equation**

Answers A - D are wrong. $(1/u)dv = -dm/m$.

Integrate: $v/u = -\ln(m/m_0)$ until the fuel is used up.

Problem 8:

(D) **The simple pendulum:** $T = 2\pi(L/g)^{1/2}$.

Problem 9:

(C) **Motion in any central potential:** Energy and angular momentum are conserved.

Problem 12:

(E) **The parallel axis theorem:** $I = MR^2 + MR^2 = 2MR^2$.